

Learning to generalize: meta-learning for domain generalization

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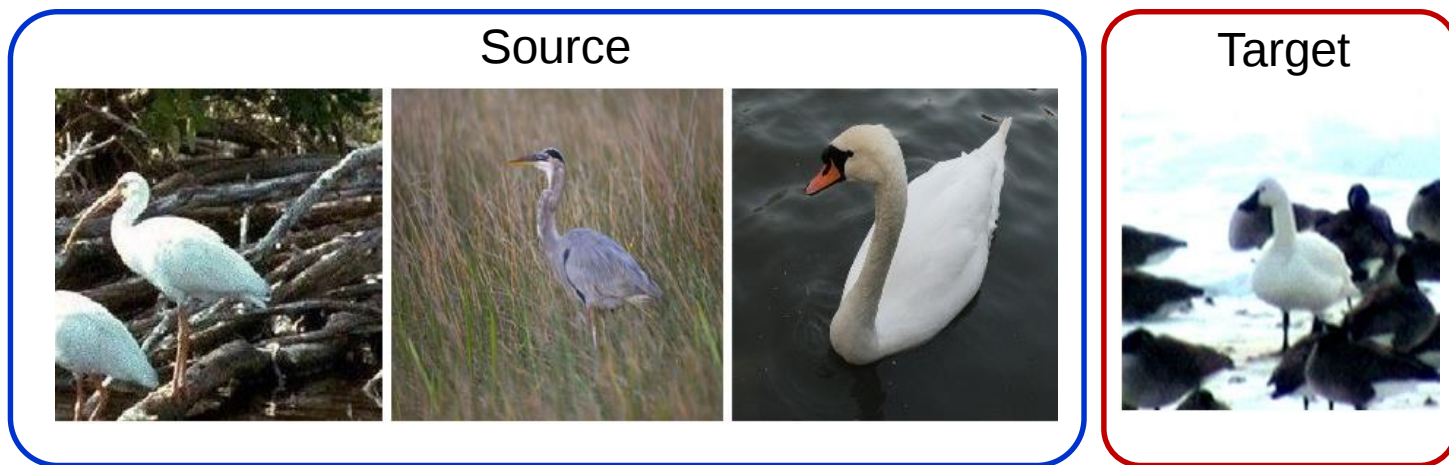
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Domain Generalization

- *What* is domain generalization?
 - Domain generalization (DG) assumes a model is trained from multiple observed (source) domains while it is expected to perform well on any unseen (target) domains.

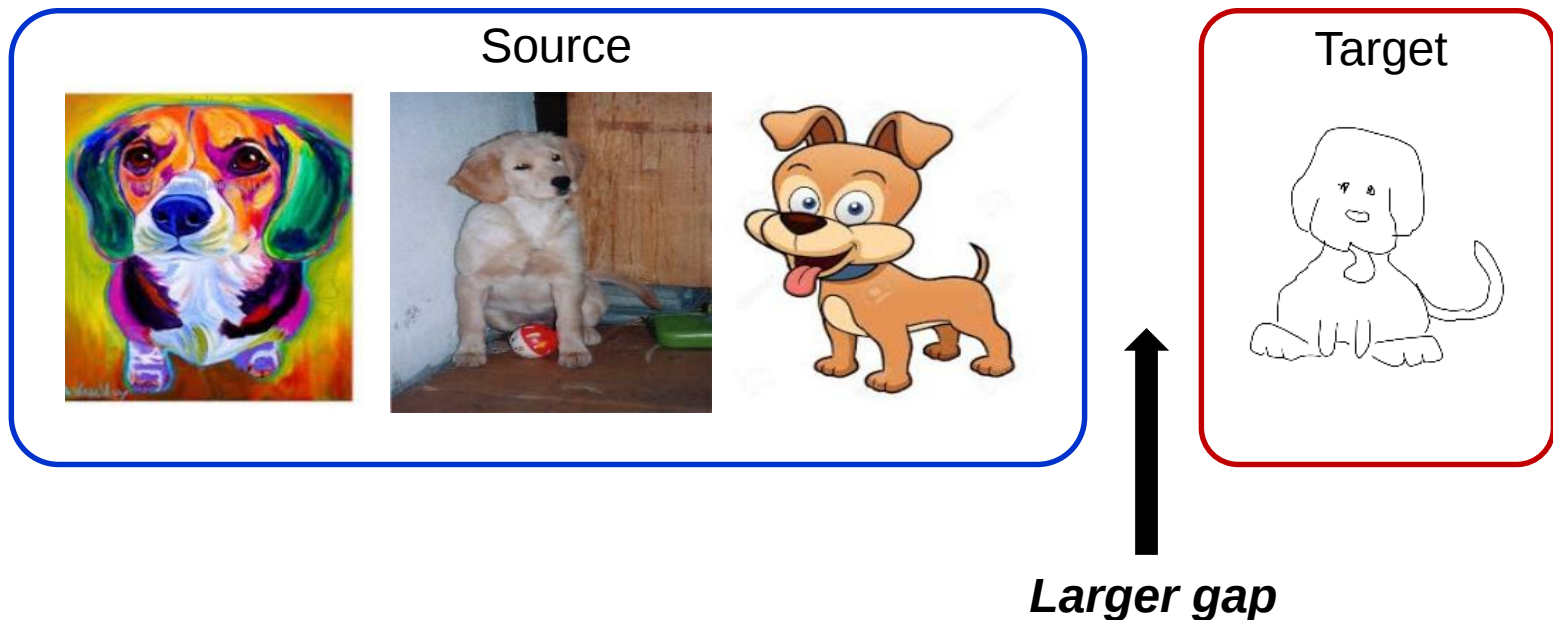
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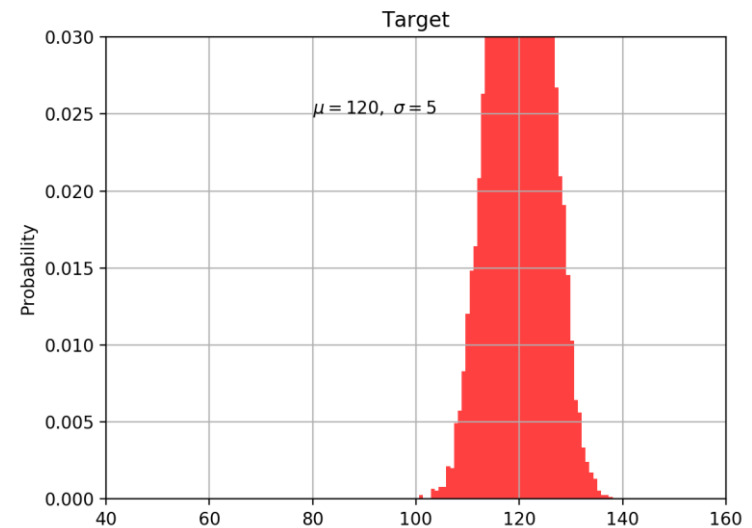
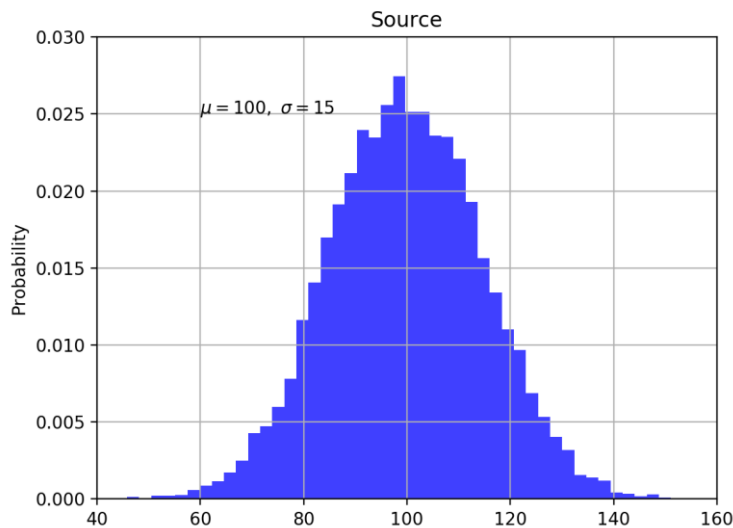
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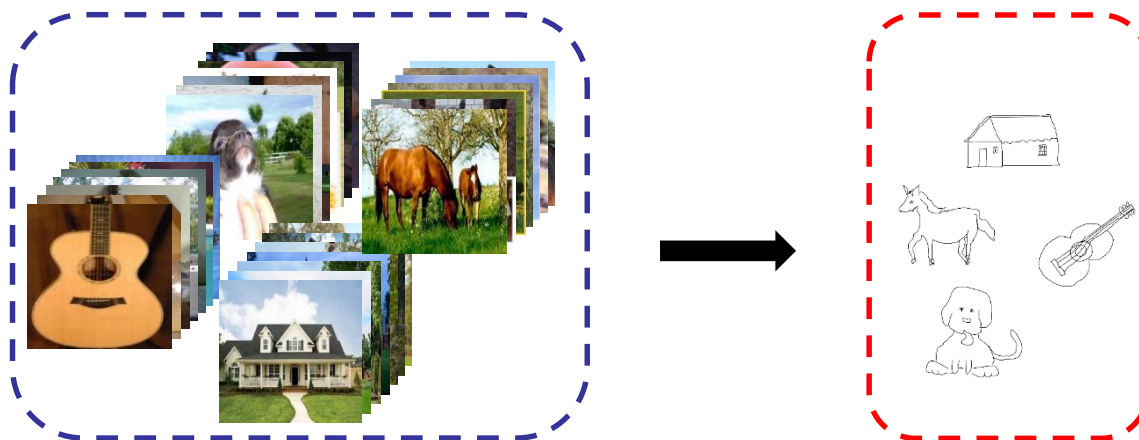
Domain Generalization

- *Why* DG is useful?
 - Data distribution shift could not be avoided, DG helps to solve this problem.



Domain Generalization

- *Why* DG is useful?
 - Data distribution shift could not be avoided, DG helps to solve this problem.
 - For the data (domain) of interest, but with too sparse data to train a good model, eg, Sketch. DG helps to train the model from the domain with large scale data, eg, Photo.



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- *How to reach DG?*
 - Domain invariant feature learning.
 - [Muandet et al, ICML'13] *~Kernel*

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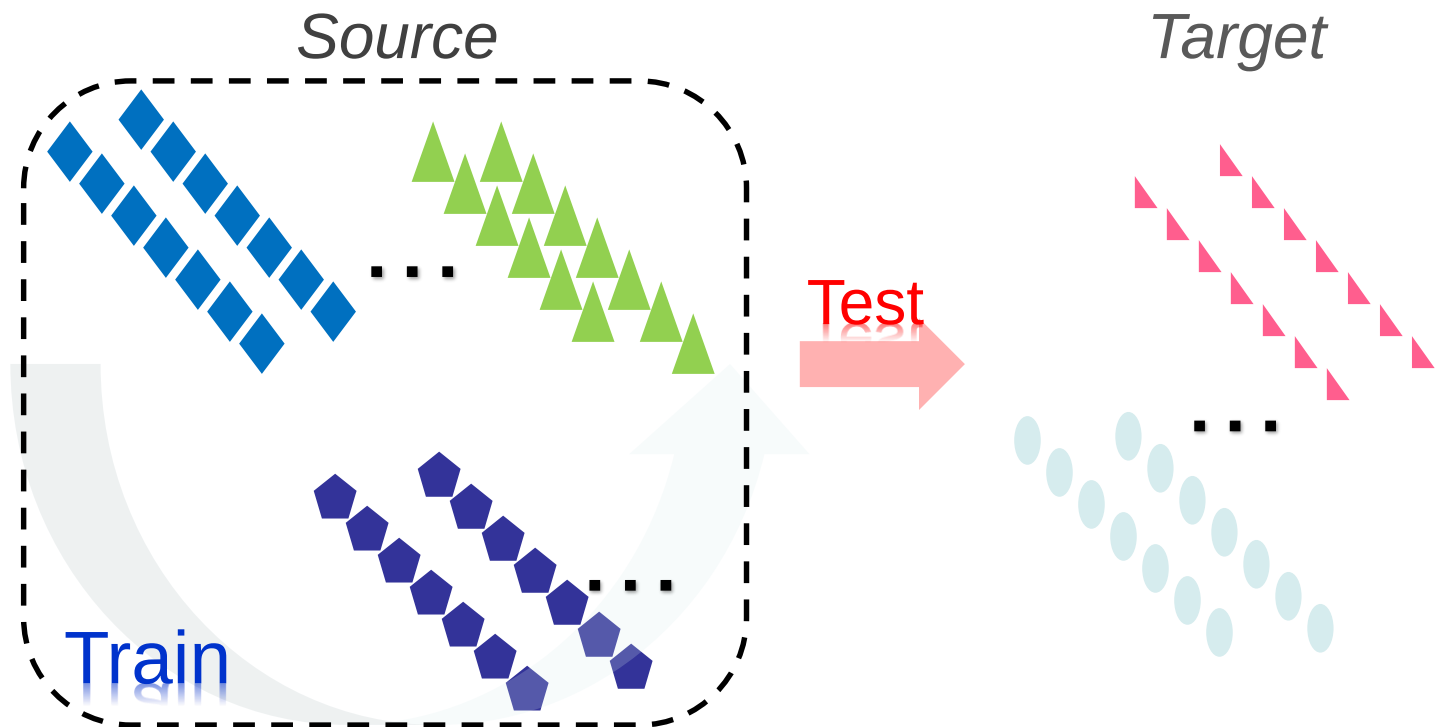
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 - Data augmentation. [Shankar et al, ICLR'18] ~*Bayesian Network*

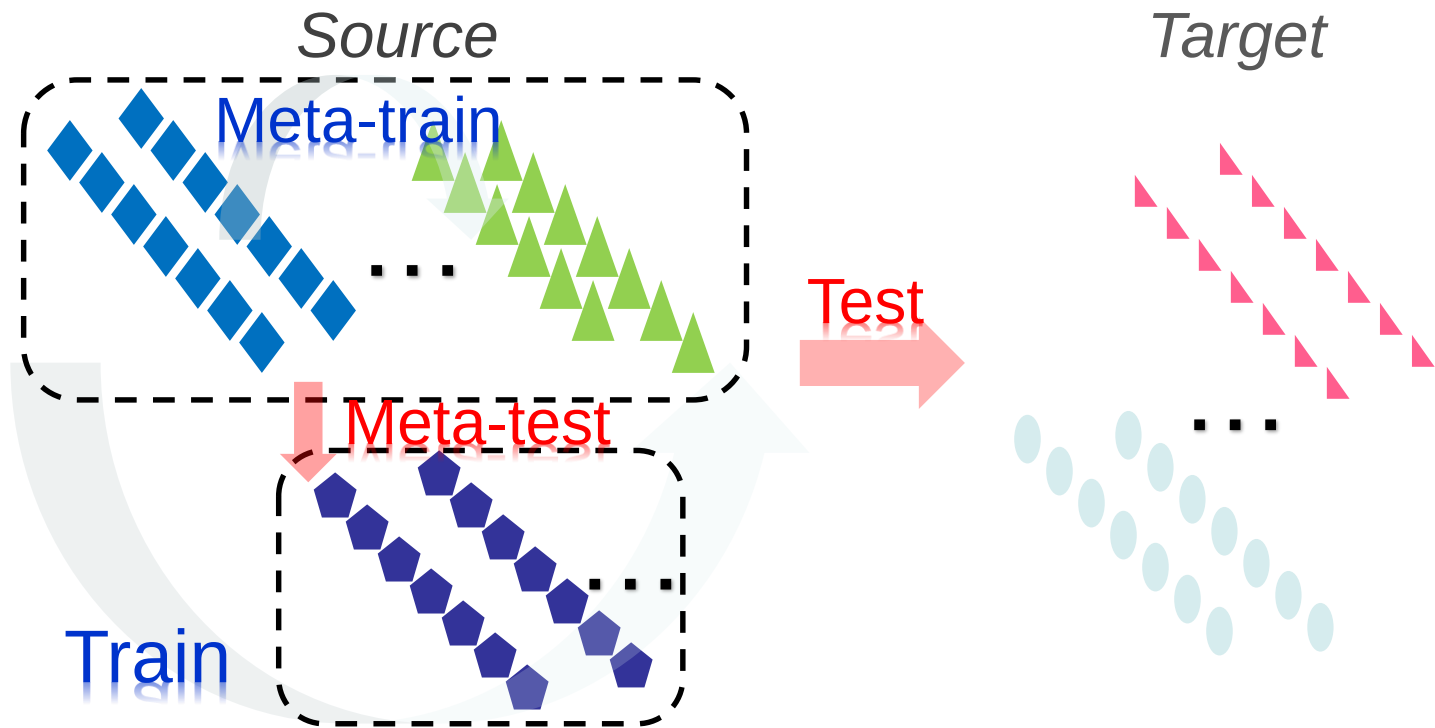
Learning to Generalize

- Conventional methods.



Learning to Generalize

- MLDG method.



Supervised Learning

- Meta-learning DG in supervised learning scenario.

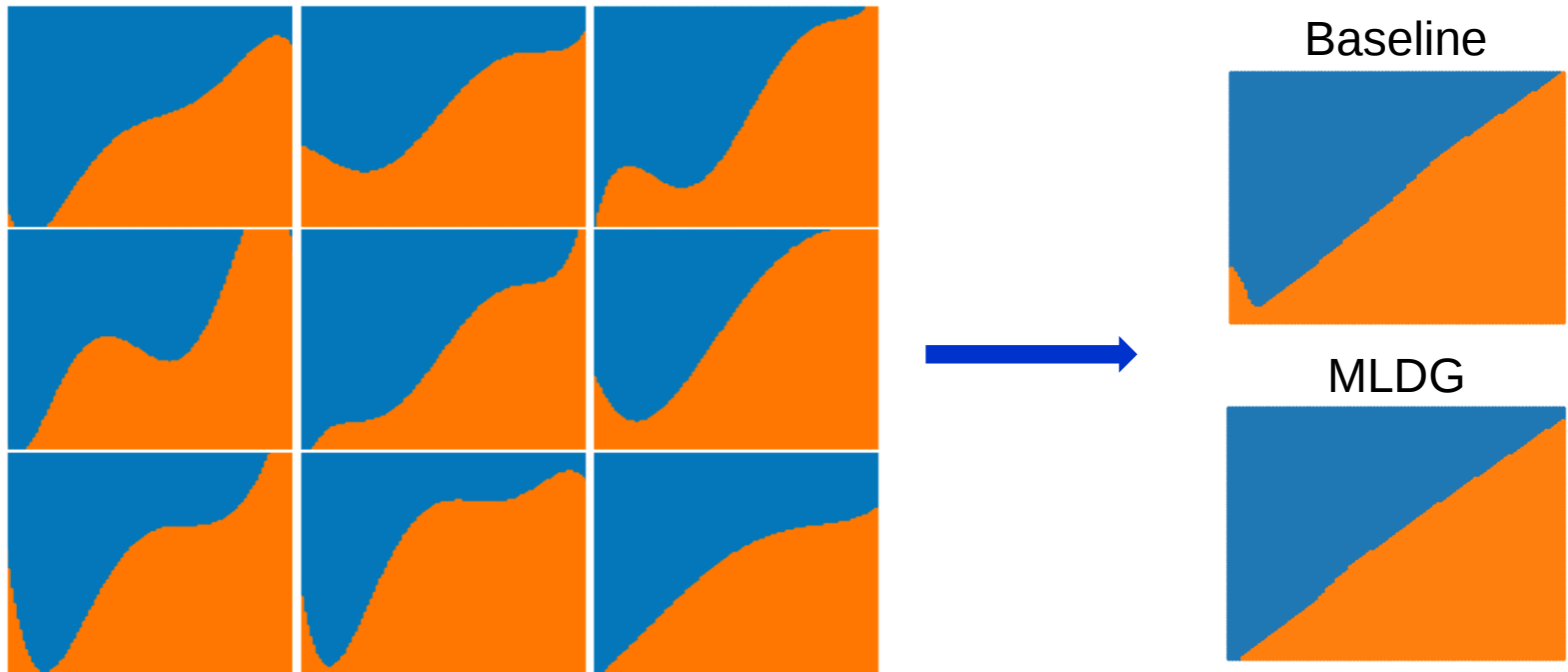
Algorithm 1 Meta-Learning Domain Generalization

```
1: procedure MLDG
2:   Input: Domains  $\mathcal{S}$ 
3:   Init: Model parameters  $\Theta$ . Hyperparameters  $\alpha, \beta, \gamma$ .
4:   for ite in iterations do
5:     Split:  $\bar{\mathcal{S}}$  and  $\check{\mathcal{S}} \leftarrow \mathcal{S}$ 
6:     Meta-train: Gradients  $\nabla_{\Theta} = \mathcal{F}'_{\Theta}(\bar{\mathcal{S}}; \Theta)$ 
7:     Updated parameters  $\Theta' = \Theta - \alpha \nabla_{\Theta}$ 
8:     Meta-test: Loss is  $\mathcal{G}(\check{\mathcal{S}}; \Theta')$ .
9:     Meta-optimization: Update  $\Theta$ 
```

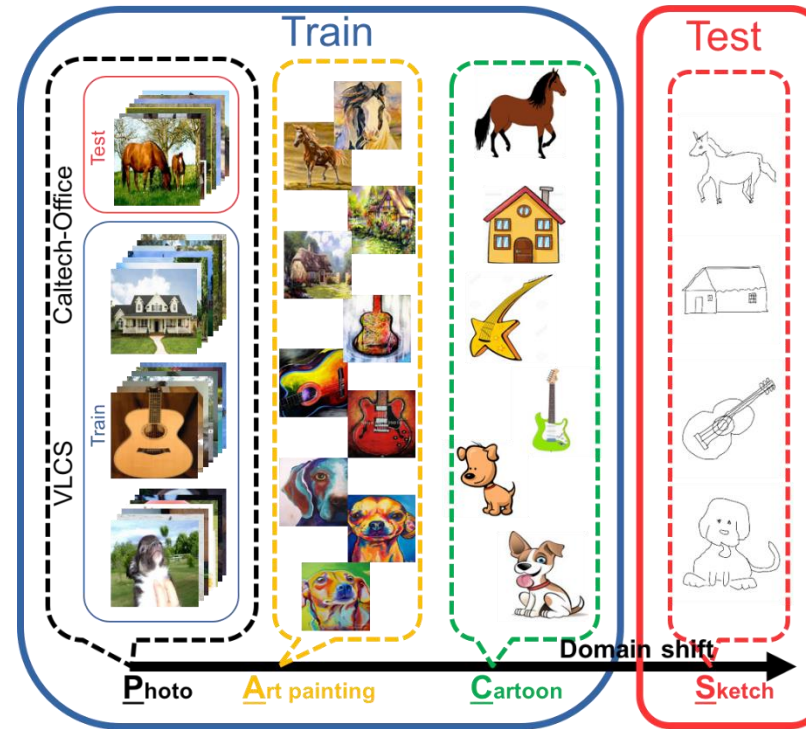
$$\Theta = \Theta - \gamma \frac{\partial(\mathcal{F}(\bar{\mathcal{S}}; \Theta) + \beta \mathcal{G}(\check{\mathcal{S}}; \Theta - \alpha \nabla_{\Theta}))}{\partial \Theta}$$

```
10:   end for
11: end procedure
```

Supervised Learning – Synthetic experiment



Supervised Learning – PACS



	D-MTAE (Ghifary et al. 2015)	Deep-all	DSN (Bousmalis et al. 2016)	AlexNet+TF (Li et al. 2017)	MLDG (CNN)
art_painting	60.27	64.91	61.13	62.86	66.23
cartoon	58.65	64.28	66.54	66.97	66.88
photo	91.12	86.67	83.25	89.50	88.00
sketch	47.86	53.08	58.58	57.51	58.96
Ave.	64.48	67.24	67.37	69.21	70.01

<https://domaingeneralization.github.io>

Taylor Series (first order)

$$\begin{array}{ccc} \text{meta-train loss} & & \text{meta-test loss} \\ \downarrow & & \downarrow \\ \operatorname{argmin}_{\Theta} \mathcal{F}(\Theta) + \beta \mathcal{G}(\Theta - \alpha \mathcal{F}'(\Theta)) \end{array}$$

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Taylor Series (first order)

meta-train loss meta-test loss

↓ ↓

$$\operatorname{argmin}_{\Theta} \mathcal{F}(\Theta) + \beta \mathcal{G}(\Theta - \alpha \mathcal{F}'(\Theta))$$

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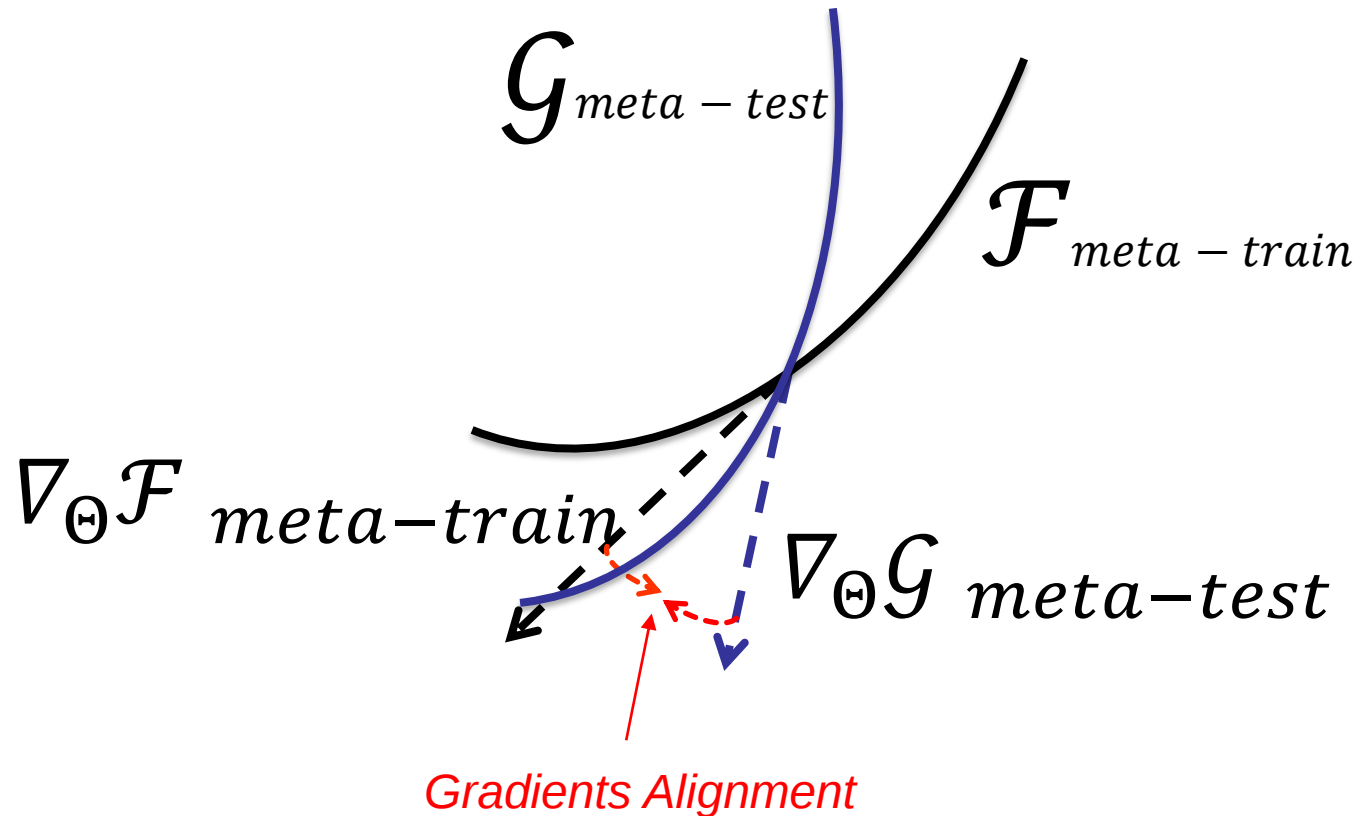
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$$\mathcal{G}(\Theta - \alpha \mathcal{F}'(\Theta)) = \mathcal{G}(\Theta) + \mathcal{G}'(\Theta) \cdot (-\alpha \mathcal{F}'(\Theta))$$

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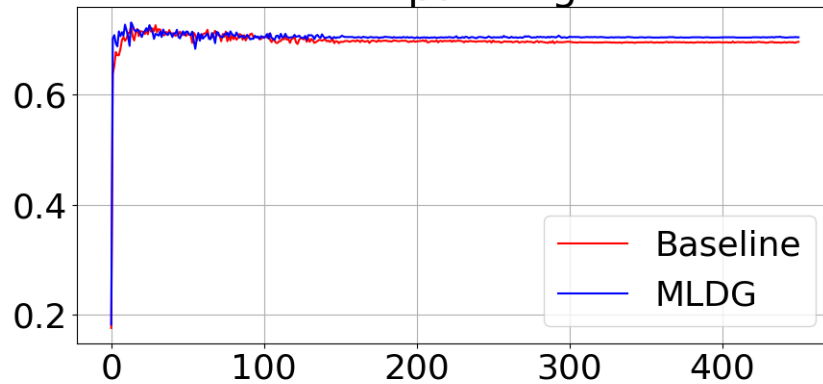
$$\operatorname{argmin}_{\Theta} \mathcal{F}(\Theta) + \beta \mathcal{G}(\Theta) - \beta \alpha (\mathcal{G}'(\Theta) \cdot \mathcal{F}'(\Theta))$$

Gradients Alignment

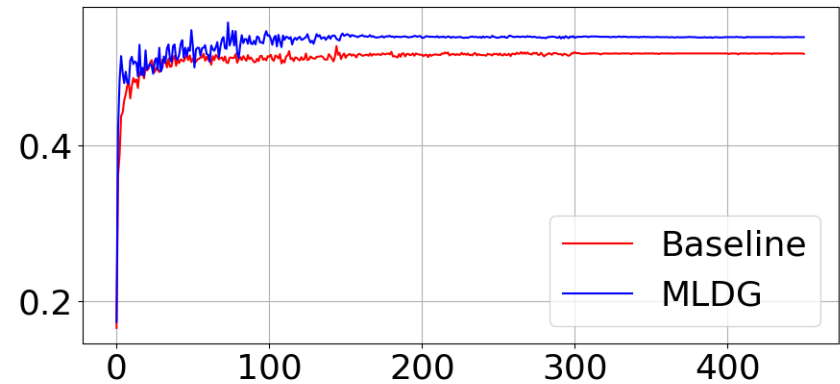


Test performance curve

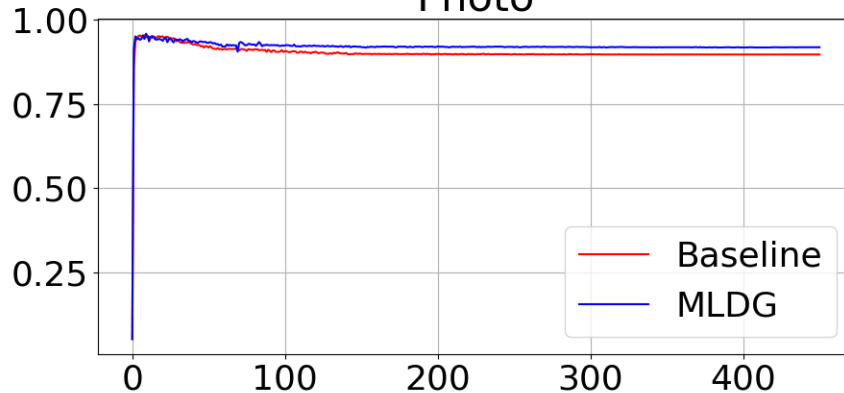
Art painting



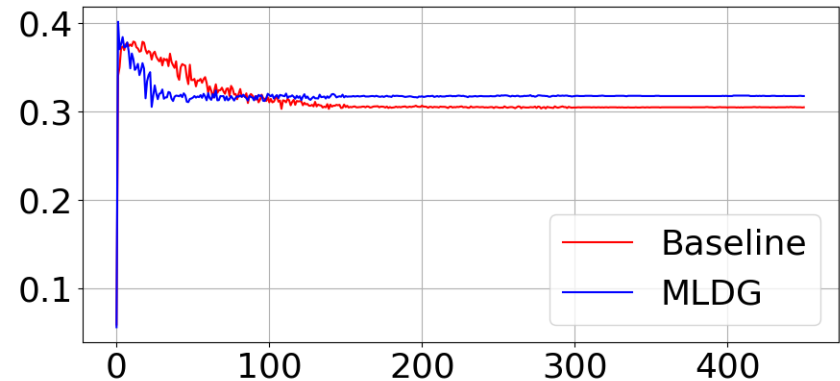
Cartoon



Photo



Sketch



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$$\operatorname{argmin}_{\Theta} \mathcal{F}(\Theta) + \beta \mathcal{G}(\Theta) - \beta \alpha \frac{\mathcal{F}'(\Theta) \cdot \mathcal{G}'(\Theta)}{\|\mathcal{F}'(\Theta)\|_2 \|\mathcal{G}'(\Theta)\|_2}$$

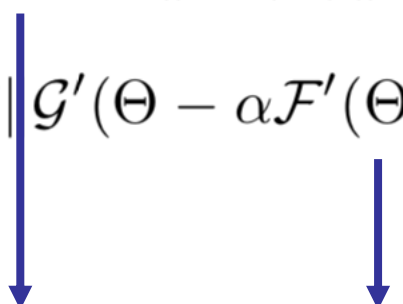
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 \downarrow & & \\
 \operatorname{argmin}_{\Theta} \mathcal{F}(\Theta) + \beta \mathcal{G}(\Theta) - \beta \alpha \frac{\mathcal{F}'(\Theta) \cdot \mathcal{G}'(\Theta)}{\|\mathcal{F}'(\Theta)\|_2 \|\mathcal{G}'(\Theta)\|_2} & & \\
 \downarrow & & \\
 \operatorname{argmin}_{\Theta} \mathcal{F}(\Theta) + \beta \|\mathcal{G}'(\Theta - \alpha \mathcal{F}'(\Theta))\|_2^2 & &
 \end{array}$$

Variants

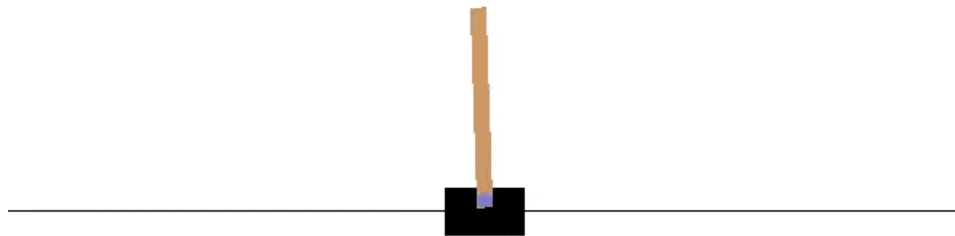
$$\operatorname{argmin}_{\Theta} \mathcal{F}(\Theta) + \beta \mathcal{G}(\Theta) - \beta \alpha \frac{\mathcal{F}'(\Theta) \cdot \mathcal{G}'(\Theta)}{\|\mathcal{F}'(\Theta)\|_2 \|\mathcal{G}'(\Theta)\|_2}$$

$$\operatorname{argmin}_{\Theta} \mathcal{F}(\Theta) + \beta \|\mathcal{G}'(\Theta - \alpha \mathcal{F}'(\Theta))\|_2^2$$



	Deep-All	MLDG-GC (Eq. 8)	MLDG-GN (Eq. 9)
art_painting	64.91	64.71	63.64
cartoon	64.28	65.30	63.47
photo	86.67	86.79	87.88
sketch	53.08	56.92	54.94
Ave.	67.24	68.43	67.48

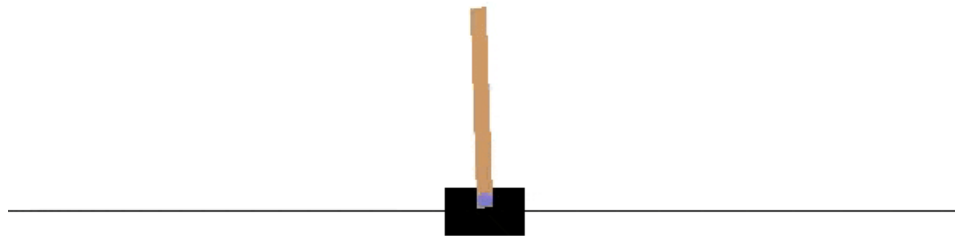
Reinforcement Learning – Cart pole



Method	RL-Random-Source	RL-All	RL-Undobias
Return	133.74 ± 6.79	97.39 ± 73.49	113.52 ± 11.65
Method	RL-MLDG	RL-MLDG-GC	RL-MLDG-GN
Return	165.34 ± 3.38	129.56 ± 2.51	175.25 ± 3.16

Across pole length. Return: reward score (upper bound=200)

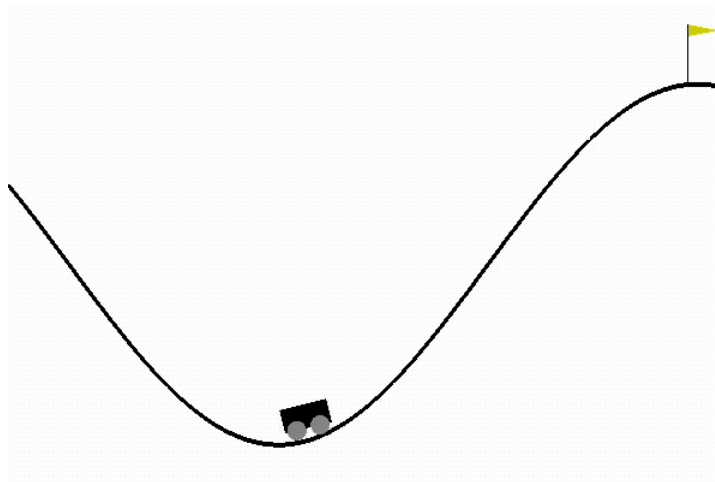
Reinforcement Learning – Cart pole



Method	RL-Random-Source	RL-All	RL-Undobias
Return	98.22 ± 20.35	144.21 ± 9.23	150.46 ± 17.59
Method	RL-MLDG	RL-MLDG-GC	RL-MLDG-GN
Return	170.81 ± 9.90	147.76 ± 4.41	164.97 ± 8.45

Across pole length and cart mass. Return: reward score (upper bound=200)

Reinforcement Learning – Mountain car



Mountain Car	RL-Random-Source	RL-All	RL-Undobias
Avg. F Rate	0.55 ± 0.07	0.05 ± 0.02	0.08 ± 0.04
Avg. Return	-191.07 ± 3.01	-141.35 ± 2.64	-124.48 ± 3.22
Mountain Car	RL-MLDG	RL-MLDG-GC	RL-MLDG-GN
Avg. F Rate	0.05 ± 0.02	0.0 ± 0.0	1.0 ± 0.0
Avg. Return	-125.73 ± 2.76	-311.80 ± 3.92	-

Across mountain height. Return: negative reward score

Thank you!